

Zero-Knowledge Age Restriction for GNU Taler

Özgür Kesim, Christian Grothoff,
Florian Dold, Martin Schanzenbach

FU Berlin, BFH Bern, Taler Systems SA, Fraunhofer AISEC

September 26, 2022

ESORICS 2022

Age restriction in E-commerce

Problem:

Verification of minimum age requirements in e-commerce.

Common solutions:

1. ID Verification
2. Restricted Accounts
3. Attribute-based

Age restriction in E-commerce

Problem:

Verification of minimum age requirements in e-commerce.

Common solutions:

Privacy

- | | |
|------------------------|------|
| 1. ID Verification | bad |
| 2. Restricted Accounts | bad |
| 3. Attribute-based | good |

Age restriction in E-commerce

Problem:

Verification of minimum age requirements in e-commerce.

Common solutions:

	Privacy	Ext. authority
1. ID Verification	bad	required
2. Restricted Accounts	bad	required
3. Attribute-based	good	required

Age restriction in E-commerce

Problem:

Verification of minimum age requirements in e-commerce.

Common solutions:

	Privacy	Ext. authority
1. ID Verification	bad	required
2. Restricted Accounts	bad	required
3. Attribute-based	good	required

Principle of Subsidiarity is violated

Principle of Subsidiarity

Functions of government—such as granting and restricting rights—should be performed *at the lowest level of authority possible*, as long as they can be performed *adequately*.

Principle of Subsidiarity

Functions of government—such as granting and restricting rights—should be performed *at the lowest level of authority possible*, as long as they can be performed *adequately*.

For age-restriction, the lowest level of authority is:

Parents, guardians and caretakers

Our contribution

Design and implementation of an age restriction scheme with the following goals:

1. It ties age restriction to the **ability to pay** (not to ID's)
2. maintains **anonymity of buyers**
3. maintains **unlinkability of transactions**
4. aligns with **principle of subsidiarity**
5. is **practical and efficient**

Age restriction

Assumptions and scenario

- ▶ Assumption: Checking accounts are under control of eligible adults/guardians.

Age restriction

Assumptions and scenario

- ▶ Assumption: Checking accounts are under control of eligible adults/guardians.
- ▶ *Guardians* **commit** to an maximum age

Age restriction

Assumptions and scenario

- ▶ Assumption: Checking accounts are under control of eligible adults/guardians.
- ▶ *Guardians* **commit** to a maximum age
- ▶ *Minors* **attest** their adequate age

Age restriction

Assumptions and scenario

- ▶ Assumption: Checking accounts are under control of eligible adults/guardians.
- ▶ *Guardians* **commit** to an maximum age
- ▶ *Minors* **attest** their adequate age
- ▶ *Merchants* **verify** the attestations

Age restriction

Assumptions and scenario

- ▶ Assumption: Checking accounts are under control of eligible adults/guardians.
- ▶ *Guardians* **commit** to an maximum age
- ▶ *Minors* **attest** their adequate age
- ▶ *Merchants* **verify** the attestations
- ▶ Minors **derive** age commitments from existing ones

Age restriction

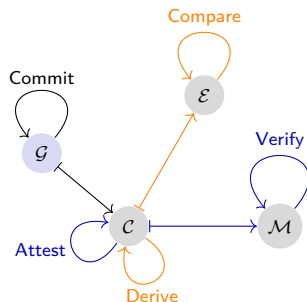
Assumptions and scenario

- ▶ Assumption: Checking accounts are under control of eligible adults/guardians.
- ▶ *Guardians* **commit** to an maximum age
- ▶ *Minors* **attest** their adequate age
- ▶ *Merchants* **verify** the attestations
- ▶ Minors **derive** age commitments from existing ones
- ▶ *Exchanges* **compare** the derived age commitments

Age restriction

Assumptions and scenario

- ▶ Assumption: Checking accounts are under control of eligible adults/guardians.
- ▶ *Guardians* **commit** to an maximum age
- ▶ *Minors* **attest** their adequate age
- ▶ *Merchants* **verify** the attestations
- ▶ Minors **derive** age commitments from existing ones
- ▶ *Exchanges* **compare** the derived age commitments



Note: Scheme is independent of payment service protocol.

Formal Function Signatures

Searching for functions

Commit

Attest

Verify

Derive

Compare

Formal Function Signatures

Searching for functions with the following signatures

Commit : $(a, \omega) \mapsto (Q, P)$ $\mathbb{N}_M \times \Omega \rightarrow \mathbb{O} \times \mathbb{P}$,

Attest

Verify

Derive

Compare

Mnemonics:

$\mathbb{O} = c\mathbb{O}mmitments$, $Q = Q\text{-}mitment$ (commitment), $\mathbb{P} = \mathbb{P}roofs$,

Formal Function Signatures

Searching for functions with the following signatures

Commit :	$(a, \omega) \mapsto (Q, P)$	$N_M \times \Omega \rightarrow O \times P,$
Attest :	$(m, Q, P) \mapsto T$	$N_M \times O \times P \rightarrow TU\{\perp\},$
Verify		
Derive		
Compare		

Mnemonics:

$O = cO$ mmits, $Q = Q$ -mitment (commitment), $P = P$ roofs, $P = P$ roof,
 $T = aT$ testations, $T = aT$ testation,

Formal Function Signatures

Searching for functions with the following signatures

Commit :	$(a, \omega) \mapsto (Q, P)$	$\mathbb{N}_M \times \Omega \rightarrow \mathbb{O} \times \mathbb{P},$
Attest :	$(m, Q, P) \mapsto T$	$\mathbb{N}_M \times \mathbb{O} \times \mathbb{P} \rightarrow \mathbb{T} \cup \{\perp\},$
Verify :	$(m, Q, T) \mapsto b$	$\mathbb{N}_M \times \mathbb{O} \times \mathbb{T} \rightarrow \mathbb{Z}_2,$
Derive		
Compare		

Mnemonics:

$\mathbb{O} = c\mathbb{O}mmitments$, $Q = Q\text{-}mitment$ (commitment), $\mathbb{P} = \mathbb{P}roofs$, $P = \mathbb{P}roof$,
 $\mathbb{T} = a\mathbb{T}testations$, $T = a\mathbb{T}testation$,

Formal Function Signatures

Searching for functions with the following signatures

Commit :	$(a, \omega) \mapsto (Q, P)$	$\mathbb{N}_M \times \Omega \rightarrow \mathbb{O} \times \mathbb{P},$
Attest :	$(m, Q, P) \mapsto T$	$\mathbb{N}_M \times \mathbb{O} \times \mathbb{P} \rightarrow \mathbb{T} \cup \{\perp\},$
Verify :	$(m, Q, T) \mapsto b$	$\mathbb{N}_M \times \mathbb{O} \times \mathbb{T} \rightarrow \mathbb{Z}_2,$
Derive :	$(Q, P, \omega) \mapsto (Q', P', \beta)$	$\mathbb{O} \times \mathbb{P} \times \Omega \rightarrow \mathbb{O} \times \mathbb{P} \times \mathbb{B},$
Compare		

Mnemonics:

$\mathbb{O} = c\mathbb{O}mmitments$, $Q = Q\text{-}mitment$ (commitment), $\mathbb{P} = \mathbb{P}roofs$, $P = \mathbb{P}roof$,
 $\mathbb{T} = a\mathbb{T}testations$, $T = a\mathbb{T}testation$, $\mathbb{B} = \mathbb{B}lindings$, $\beta = \beta\text{linding}$.

Formal Function Signatures

Searching for functions with the following signatures

Commit :	$(a, \omega) \mapsto (Q, P)$	$\mathbb{N}_M \times \Omega \rightarrow \mathbb{O} \times \mathbb{P},$
Attest :	$(m, Q, P) \mapsto T$	$\mathbb{N}_M \times \mathbb{O} \times \mathbb{P} \rightarrow \mathbb{T} \cup \{\perp\},$
Verify :	$(m, Q, T) \mapsto b$	$\mathbb{N}_M \times \mathbb{O} \times \mathbb{T} \rightarrow \mathbb{Z}_2,$
Derive :	$(Q, P, \omega) \mapsto (Q', P', \beta)$	$\mathbb{O} \times \mathbb{P} \times \Omega \rightarrow \mathbb{O} \times \mathbb{P} \times \mathbb{B},$
Compare :	$(Q, Q', \beta) \mapsto b$	$\mathbb{O} \times \mathbb{O} \times \mathbb{B} \rightarrow \mathbb{Z}_2,$

Mnemonics:

$\mathbb{O} = c\mathbb{O}mmitments$, $\mathbb{Q} = Q\text{-}mitment$ (commitment), $\mathbb{P} = \mathbb{P}roofs$, $\mathbb{P} = \mathbb{P}roof$,
 $\mathbb{T} = a\mathbb{T}testations$, $\mathbb{T} = a\mathbb{T}testation$, $\mathbb{B} = \mathbb{B}lindings$, $\beta = \beta\text{-}linding$.

Formal Function Signatures

Searching for functions with the following signatures

Commit :	$(a, \omega) \mapsto (Q, P)$	$\mathbb{N}_M \times \Omega \rightarrow \mathbb{O} \times \mathbb{P},$
Attest :	$(m, Q, P) \mapsto T$	$\mathbb{N}_M \times \mathbb{O} \times \mathbb{P} \rightarrow \mathbb{T} \cup \{\perp\},$
Verify :	$(m, Q, T) \mapsto b$	$\mathbb{N}_M \times \mathbb{O} \times \mathbb{T} \rightarrow \mathbb{Z}_2,$
Derive :	$(Q, P, \omega) \mapsto (Q', P', \beta)$	$\mathbb{O} \times \mathbb{P} \times \Omega \rightarrow \mathbb{O} \times \mathbb{P} \times \mathbb{B},$
Compare :	$(Q, Q', \beta) \mapsto b$	$\mathbb{O} \times \mathbb{O} \times \mathbb{B} \rightarrow \mathbb{Z}_2,$

with $\Omega, \mathbb{P}, \mathbb{O}, \mathbb{T}, \mathbb{B}$ sufficiently large sets.

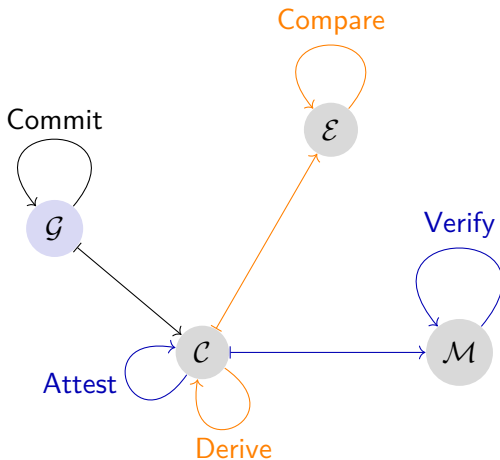
Basic and security requirements are defined later.

Mnemonics:

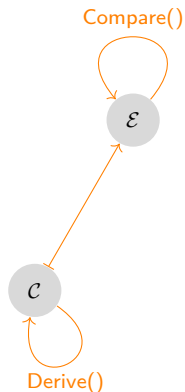
$\mathbb{O} = c\mathbb{O}mmitments$, $Q = Q\text{-}mitment$ (commitment), $\mathbb{P} = \mathbb{P}roofs$, $P = P\text{roof}$,
 $\mathbb{T} = a\mathbb{T}testations$, $T = a\mathbb{T}testation$, $\mathbb{B} = \mathbb{B}lindings$, $\beta = \beta\text{linding}$.

Age restriction

Naïve scheme

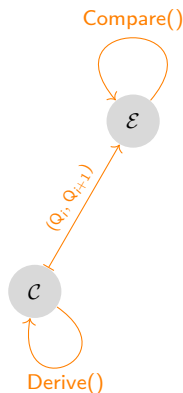


Achieving Unlinkability



Simple use of `Derive()` and `Compare()` is problematic.

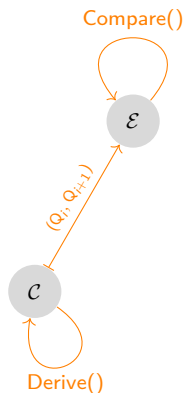
Achieving Unlinkability



Simple use of `Derive()` and `Compare()` is problematic.

- ▶ Calling `Derive()` iteratively generates sequence (Q_0, Q_1, \dots) of commitments.
- ▶ Exchange calls `Compare(Q_i, Q_{i+1}, \dots)`

Achieving Unlinkability



Simple use of $Derive()$ and $Compare()$ is problematic.

- ▶ Calling $Derive()$ iteratively generates sequence (Q_0, Q_1, \dots) of commitments.
- ▶ Exchange calls $Compare(Q_i, Q_{i+1}, \dots)$

⇒ **Exchange identifies sequence**

⇒ **Unlinkability broken**

Achieving Unlinkability

Define cut&choose protocol $\text{DeriveCompare}_\kappa$, using $\text{Derive}()$ and $\text{Compare}()$.

Achieving Unlinkability

Define cut&choose protocol **DeriveCompare $_{\kappa}$** , using `Derive()` and `Compare()`.

Sketch:

1. \mathcal{C} derives commitments (Q_1, \dots, Q_{κ}) from Q_0 by calling `Derive()` with bindings $(\beta_1, \dots, \beta_{\kappa})$
2. \mathcal{C} calculates $h_0 := H(H(Q_1, \beta_1) || \dots || H(Q_{\kappa}, \beta_{\kappa}))$
3. \mathcal{C} sends Q_0 and h_0 to \mathcal{E}
4. \mathcal{E} chooses $\gamma \in \{1, \dots, \kappa\}$ randomly
5. \mathcal{C} reveals $h_{\gamma} := H(Q_{\gamma}, \beta_{\gamma})$ and all (Q_i, β_i) , except $(Q_{\gamma}, \beta_{\gamma})$
6. \mathcal{E} compares h_0 and $H(H(Q_1, \beta_1) || \dots || h_{\gamma} || \dots || H(Q_{\kappa}, \beta_{\kappa}))$ and evaluates `Compare`(Q_0, Q_i, β_i).

Note: Scheme is similar to the *refresh* protocol in GNU Taler.

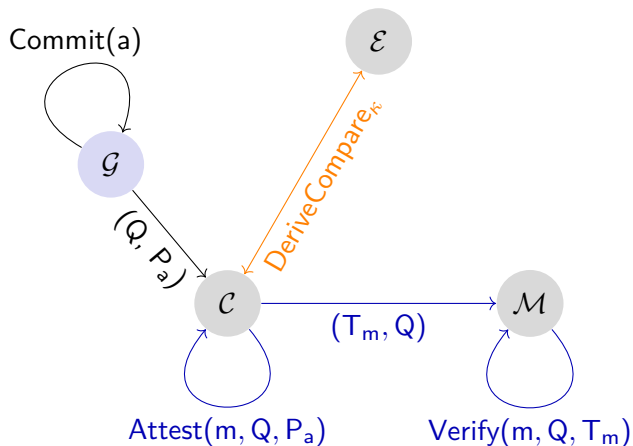
Achieving Unlinkability

With `DeriveCompare κ`

- ▶ \mathcal{E} learns nothing about Q_γ ,
- ▶ trusts outcome with $\frac{\kappa-1}{\kappa}$ certainty,
- ▶ i.e. \mathcal{C} has $\frac{1}{\kappa}$ chance to cheat.

Note: Still need Derive and Compare to be defined.

Refined scheme



Basic Requirements

Candidate functions

(Commit, Attest, Verify, Derive, Compare)

must first meet *basic* requirements:

- ▶ Existence of attestations
- ▶ Efficacy of attestations
- ▶ Derivability of commitments and attestations

Basic Requirements

Formal Details

Existence of attestations

$$\forall_{\substack{a \in \mathbb{N}_M \\ \omega \in \Omega}} : \text{Commit}(a, \omega) =: (Q, P) \implies \text{Attest}(m, Q, P) = \begin{cases} T \in \mathbb{T}, & \text{if } m \leq a \\ \perp & \text{otherwise} \end{cases}$$

Efficacy of attestations

$$\text{Verify}(m, Q, T) = \begin{cases} 1, & \text{if } \exists_{P \in \mathbb{P}} : \text{Attest}(m, Q, P) = T \\ 0 & \text{otherwise} \end{cases}$$

$$\forall_{n \leq a} : \text{Verify}(n, Q, \text{Attest}(n, Q, P)) = 1.$$

etc.

Security Requirements

Candidate functions must also meet *security* requirements. Those are defined via security games:

- ▶ Game: Age disclosure by commitment or attestation
↔ Requirement: Non-disclosure of age
- ▶ Game: Forging attestation
↔ Requirement: Unforgeability of minimum age
- ▶ Game: Distinguishing derived commitments and attestations
↔ Requirement: Unlinkability of commitments and attestations

Meeting the security requirements means that adversaries can win those games only with negligible advantage.

Adversaries are arbitrary polynomial-time algorithms, acting on all relevant input.

Security Requirements

Simplified Example

Game $G_A^{\text{FA}}(\lambda)$ —Forging an attest:

1. $(a, \omega) \xleftarrow{\$} \mathbb{N}_{M-1} \times \Omega$
2. $(Q, P) \leftarrow \text{Commit}(a, \omega)$
3. $(m, T) \leftarrow \mathcal{A}(a, Q, P)$
4. Return 0 if $m \leq a$
5. Return $\text{Verify}(m, Q, T)$

Requirement: Unforgeability of minimum age

$$\forall \mathcal{A} \in \mathfrak{A}(\mathbb{N}_M \times \mathbb{O} \times \mathbb{P} \rightarrow \mathbb{N}_M \times \mathbb{T}) : \Pr \left[G_A^{\text{FA}}(\lambda) = 1 \right] \leq \epsilon(\lambda)$$

Solution: Instantiation with ECDSA

To Commit to age (group) 'a'

Solution: Instantiation with ECDSA

To Commit to age (group) 'a'

1. Guardian generates ECDSA-keypairs, one per age (group):

$$\langle (q_1, p_1), \dots, (q_M, p_M) \rangle$$

Solution: Instantiation with ECDSA

To Commit to age (group) 'a'

1. Guardian generates ECDSA-keypairs, one per age (group):

$$\langle (q_1, p_1), \dots, (q_M, p_M) \rangle$$

2. Guardian then **drops** all private keys p_i for $i > a$:

$$\langle (q_1, p_1), \dots, (q_a, p_a), (q_{a+1}, \perp), \dots, (q_M, \perp) \rangle$$

- ▶ $\vec{Q} := (q_1, \dots, q_M)$ is the *Commitment*,
- ▶ $\vec{P}_a := (p_1, \dots, p_a, \perp, \dots, \perp)$ is the *Proof*

Solution: Instantiation with ECDSA

To Commit to age (group) 'a'

1. Guardian generates ECDSA-keypairs, one per age (group):

$$\langle (q_1, p_1), \dots, (q_M, p_M) \rangle$$

2. Guardian then **drops** all private keys p_i for $i > a$:

$$\langle (q_1, p_1), \dots, (q_a, p_a), (q_{a+1}, \perp), \dots, (q_M, \perp) \rangle$$

- ▶ $\vec{Q} := (q_1, \dots, q_M)$ is the *Commitment*,
- ▶ $\vec{P}_a := (p_1, \dots, p_a, \perp, \dots, \perp)$ is the *Proof*

3. Guardian gives child $\langle \vec{Q}, \vec{P}_a \rangle$

Instantiation with ECDSA

Definitions of Attest and Verify

Child has

- ▶ ordered public-keys $\vec{Q} = (q_1, \dots, q_M)$,
- ▶ (some) private-keys $\vec{P} = (p_1, \dots, p_a, \perp, \dots, \perp)$.

Instantiation with ECDSA

Definitions of Attest and Verify

Child has

- ▶ ordered public-keys $\vec{Q} = (q_1, \dots, q_M)$,
- ▶ (some) private-keys $\vec{P} = (p_1, \dots, p_a, \perp, \dots, \perp)$.

To Attest a minimum age $m \leq a$:

Sign a message with ECDSA using private key p_m

Instantiation with ECDSA

Definitions of Attest and Verify

Child has

- ▶ ordered public-keys $\vec{Q} = (q_1, \dots, q_M)$,
- ▶ (some) private-keys $\vec{P} = (p_1, \dots, p_a, \perp, \dots, \perp)$.

To Attest a minimum age $m \leq a$:

Sign a message with ECDSA using private key p_m

Merchant gets

- ▶ ordered public-keys $\vec{Q} = (q_1, \dots, q_M)$
- ▶ Signature σ

Instantiation with ECDSA

Definitions of Attest and Verify

Child has

- ▶ ordered public-keys $\vec{Q} = (q_1, \dots, q_M)$,
- ▶ (some) private-keys $\vec{P} = (p_1, \dots, p_a, \perp, \dots, \perp)$.

To Attest a minimum age $m \leq a$:

Sign a message with ECDSA using private key p_m

Merchant gets

- ▶ ordered public-keys $\vec{Q} = (q_1, \dots, q_M)$
- ▶ Signature σ

To Verify a minimum age m :

Verify the ECDSA-Signature σ with public key q_m .

Instantiation with ECDSA

Definitions of Derive and Compare

Child has $\vec{Q} = (q_1, \dots, q_M)$ and $\vec{P} = (p_1, \dots, p_a, \perp, \dots, \perp)$.

Instantiation with ECDSA

Definitions of Derive and Compare

Child has $\vec{Q} = (q_1, \dots, q_M)$ and $\vec{P} = (p_1, \dots, p_a, \perp, \dots, \perp)$.

To Derive new \vec{Q}' and \vec{P}' : Choose random $\beta \in \mathbb{Z}_g$ and calculate

$$\vec{Q}' := (\beta * q_1, \dots, \beta * q_M),$$

$$\vec{P}' := (\beta p_1, \dots, \beta p_a, \perp, \dots, \perp)$$

Note: $(\beta p_i) * G = \beta * (p_i * G) = \beta * q_i$

$\beta * q_i$ is scalar multiplication on the elliptic curve.

Instantiation with ECDSA

Definitions of Derive and Compare

Child has $\vec{Q} = (q_1, \dots, q_M)$ and $\vec{P} = (p_1, \dots, p_a, \perp, \dots, \perp)$.

To Derive new \vec{Q}' and \vec{P}' : Choose random $\beta \in \mathbb{Z}_g$ and calculate

$$\vec{Q}' := (\beta * q_1, \dots, \beta * q_M),$$

$$\vec{P}' := (\beta p_1, \dots, \beta p_a, \perp, \dots, \perp)$$

Note: $(\beta p_i) * G = \beta * (p_i * G) = \beta * q_i$

$\beta * q_i$ is scalar multiplication on the elliptic curve.

Exchange gets $\vec{Q} = (q_1, \dots, q_M)$, $\vec{Q}' = (q'_1, \dots, q'_M)$ and β

To Compare, calculate: $(\beta * q_1, \dots, \beta * q_M) \stackrel{?}{=} (q'_1, \dots, q'_M)$

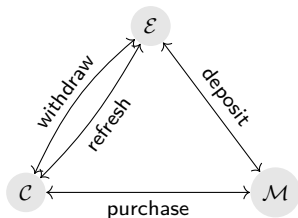
Instantiation with ECDSA

Functions (Commit, Attest, Verify, Derive, Compare)
as defined in the instantiation with ECDSA

- ▶ meet the basic requirements,
- ▶ also meet all security requirements.
Proofs by security reduction, details are in the paper.

GNU Taler

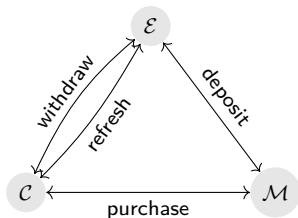
<https://www.taler.net>



- ▶ Protocol suite for online payment services
- ▶ Based on Chaum's blind signatures
- ▶ Allows for change and refund (F. Dold)
- ▶ Privacy preserving: anonymous and unlinkable payments

GNU Taler

<https://www.taler.net>



- ▶ Protocol suite for online payment services
- ▶ Based on Chaum's blind signatures
- ▶ Allows for change and refund (F. Dold)
- ▶ Privacy preserving: anonymous and unlinkable payments

- ▶ Coins are public-/private key-pairs (C_p, c_s) .
- ▶ Exchange blindly signs $\text{FDH}(C_p)$ with denomination key d_p
- ▶ Verification:

$$1 \stackrel{?}{=} \text{SigCheck}(\text{FDH}(C_p), D_p, \sigma_p)$$

(D_p = public key of denomination and σ_p = signature)

Integration with GNU Taler

Binding age restriction to coins

To bind an age commitment Q to a coin C_p , instead of signing $\text{FDH}(C_p)$, \mathcal{E} now blindly signs

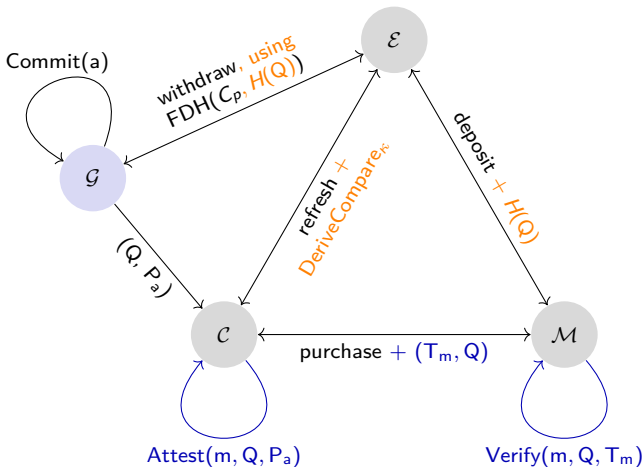
$$\text{FDH}(C_p, H(Q))$$

Verification of a coin now requires $H(Q)$, too:

$$1 \stackrel{?}{=} \text{SigCheck}(\text{FDH}(C_p, H(Q)), D_p, \sigma_p)$$

Integration with GNU Taler

Integrated schemes



Instantiation with Edx25519

Paper also formally defines another signature scheme: Edx25519.

- ▶ Scheme already in use in GNUnet,
- ▶ based on EdDSA (Bernstein et al.),
- ▶ generates compatible signatures and
- ▶ allows for key derivation from both, private and public keys, independently.

Current implementation of age restriction in GNU Taler uses Edx25519.

Discussion

- ▶ Our solution can in principle be used with any token-based payment scheme
- ▶ GNU Taler best aligned with our design goals (security, privacy and efficiency)
- ▶ Subsidiarity requires bank accounts being owned by adults
 - ▶ Scheme can be adapted to case where minors have bank accounts
 - ▶ Assumption: banks provide minimum age information during bank transactions.
 - ▶ Child and Exchange execute a variant of the cut&choose protocol.
- ▶ Our scheme offers an alternative to identity management systems (IMS)

Related Work

- ▶ Current privacy-preserving systems all based on attribute-based credentials (Koning et al., Schanzenbach et al., Camenisch et al., Au et al.)
- ▶ Attribute-based approach lacks support:
 - ▶ Complex for consumers and retailers
 - ▶ Requires trusted third authority
- ▶ Other approaches tie age-restriction to ability to pay (“debit cards for kids”)
 - ▶ Advantage: mandatory to payment process
 - ▶ Not privacy friendly

Conclusion

Age restriction is a technical, ethical and legal challenge.

Existing solutions are

- ▶ without strong protection of privacy or
- ▶ based on identity management systems (IMS)

Our scheme offers a solution that is

- ▶ based on subsidiarity
- ▶ privacy preserving
- ▶ efficient
- ▶ an alternative to IMS